


# Back-Propagation Algorithm for Deep Neural Networks and Contradictive Diverse Learning for Restricted Boltzmann Machine

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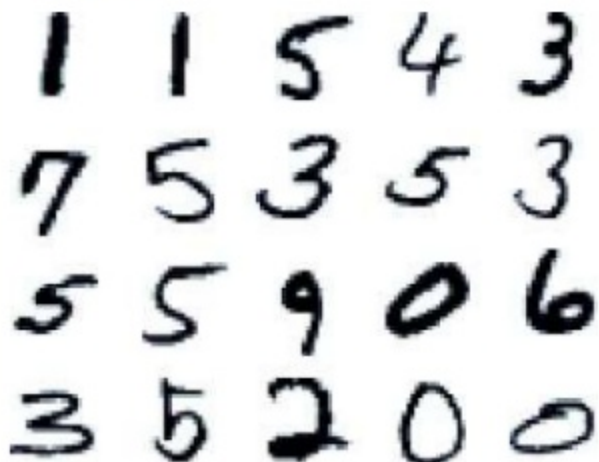


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1. Examples of Deep Learning
  2. RBM to Deep NN
  3. Deep Neural Network (Deep NN)
    - Back-Propagation (Supervised Learning)
  4. Restricted Boltzmann Machine (RBM)
    - Mathematics, Probabilistic Model and Inference Model
    - Pre-training by Contradictive Diverse Learning (Unsupervised Learning)
  5. Inference Model with Distribution

# Deep learning

- Top performance in character recognition
  - MNIST (handwritten digits benchmark)

## MNIST



Result	Method	Venue	Details
0.21%	<a href="#">Regularization of Neural Networks using DropConnect</a>	ICML 2013	
0.23%	<a href="#">Multi-column Deep Neural Networks for Image Classification</a>	CVPR 2012	
0.35%	<a href="#">Deep Big Simple Neural Nets Excel on Handwritten Digit Recognition</a>	Neural Computation 2010	<a href="#">Details</a>
0.39%	<a href="#">Efficient Learning of Sparse Representations with an Energy-Based Model</a>	NIPS 2006	<a href="#">Details</a>
0.39%	<a href="#">Convolutional Kernel Networks</a>	arXiv 2014	<a href="#">Details</a>
0.39%	<a href="#">Deeply-Supervised Nets</a>	arXiv 2014	
0.4%	<a href="#">Best Practices for Convolutional Neural Networks Applied to Visual Document Analysis</a>	Document Analysis and Recognition 2003	
0.45%	<a href="#">Maxout Networks</a>	ICML 2013	<a href="#">Details</a>
0.47%	<a href="#">Network in Network</a>	ICLR 2014	<a href="#">Details</a>
0.52 %	<a href="#">Trainable COSFIRE filters for keypoint detection and pattern recognition</a>	PAMI 2013	<a href="#">Details</a>
0.53%	<a href="#">What is the Best Multi-Stage Architecture for Object Recognition?</a>	ICCV 2009	<a href="#">Details</a>
0.54%	<a href="#">A trainable feature extractor for handwritten digit recognition</a>	Journal Pattern Recognition	<a href="#">Details</a>



# Deep learning

- Top performance in image classification
  - CIFAR (image classification benchmark)

## CIFAR10



Result	Method	Venue	Details
94%	<a href="#">Lessons learned from manually classifying CIFAR-10</a>	unpublished 2011	<a href="#">Details</a>
91.78%	<a href="#">Deeply-Supervised Nets</a>	arXiv 2014	<a href="#">Details</a>
91.2%	<a href="#">Network In Network</a>	ICLR 2014	<a href="#">Details</a>
90.68%	<a href="#">Regularization of Neural Networks using DropConnect</a>	ICML 2013	
90.65%	<a href="#">Maxout Networks</a>	ICML 2013	<a href="#">Details</a>
90.61%	<a href="#">Improving Deep Neural Networks with Probabilistic Maxout Units</a>	ICLR 2014	<a href="#">Details</a>
90.5%	<a href="#">Practical Bayesian Optimization of Machine Learning Algorithms</a>	NIPS 2012	<a href="#">Details</a>
89%	<a href="#">ImageNet Classification with Deep Convolutional Neural Networks</a>	NIPS 2012	<a href="#">Details</a>
88.79%	<a href="#">Multi-Column Deep Neural Networks for Image Classification</a>	CVPR 2012	<a href="#">Details</a>
84.87%	<a href="#">Stochastic Pooling for Regularization of Deep Convolutional Neural Networks</a>	arXiv 2013	
84.4%	<a href="#">Improving neural networks by preventing co-adaptation of feature detectors</a>	arXiv 2012	<a href="#">Details</a>
83.96%	<a href="#">Discriminative Learning of Sum-Product Networks</a>	NIPS 2012	
82.9%	<a href="#">Stable and Efficient Representation Learning with Nonnegativity Constraints</a>	ICML 2014	<a href="#">Details</a>

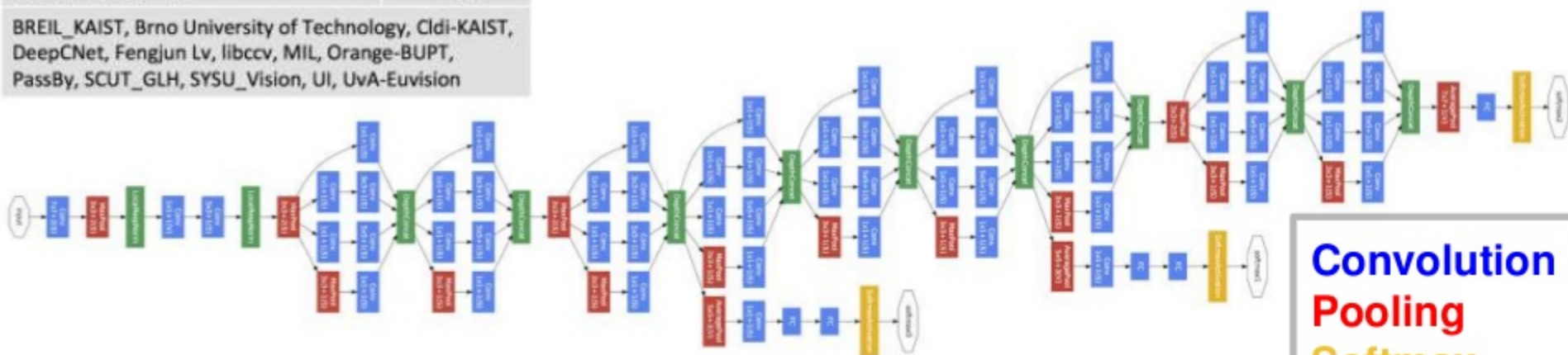
# Deep learning

## ➤ Top performance in visual recognition

Team Name	Error (%)
GoogLeNet	6.7
VGG	7.3
MSRA Visual computing	8.1
Andrew Howard	8.1
DeeperVision	9.5
NUS-BST	9.8
TTIC_ECP – Epitomic Vision	10.2
XYZ	11.2
BDC-I2R-UPMC	11.3

BREIL\_KAIST, Brno University of Technology, Cldi-KAIST, DeepCNet, Fengjun Lv, libccv, MIL, Orange-BUPT, PassBy, SCUT\_GLH, SYSU\_Vision, UI, UvA-Euvison

Image Large Scale Visual Recognition Challenge (ILSVRC)



GoogLeNet, ILSVRC2014

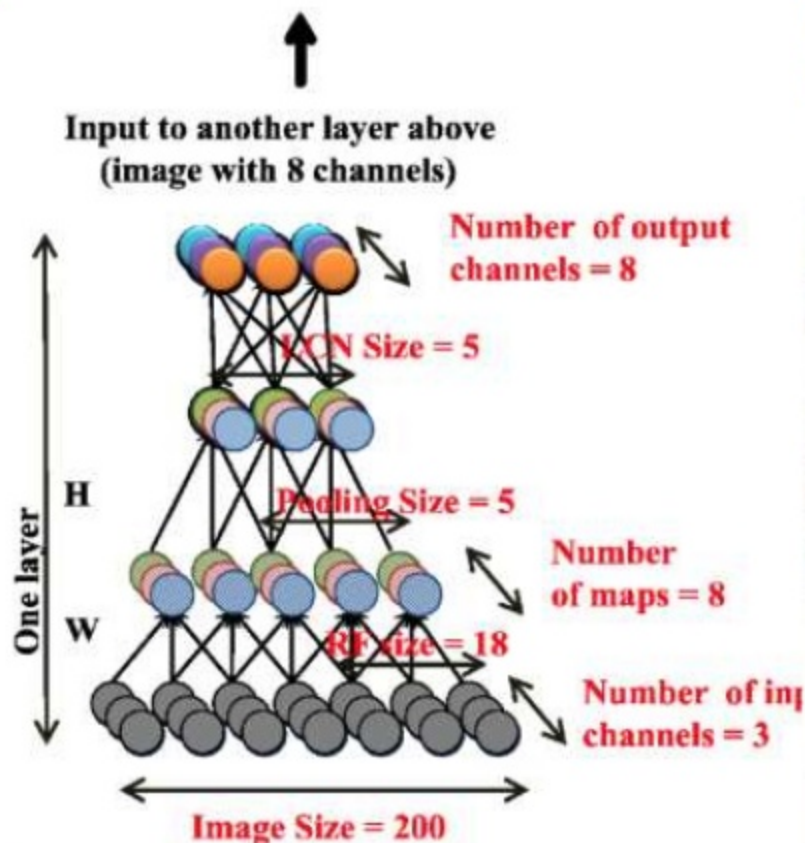
**Convolution**  
**Pooling**  
**Softmax**  
**Other**



# Deep learning

## ➤ “Cat neuron”

Automatic learning with youtube videos,  
neuron for human's face  
neuron for cat



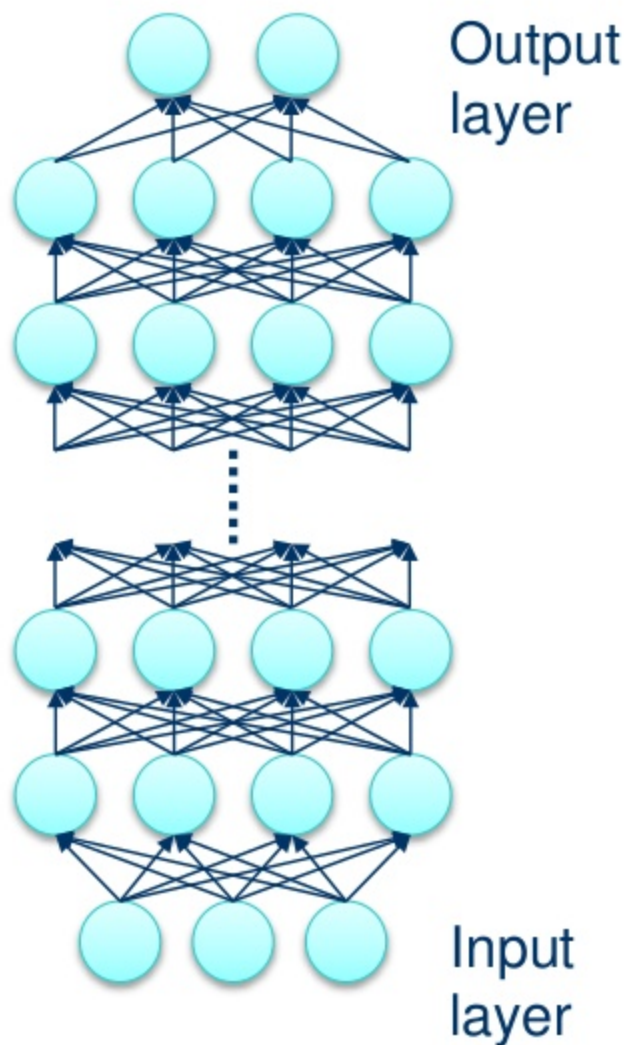
10,000,000:  
training samples

Three days learning with  
1,000 computers

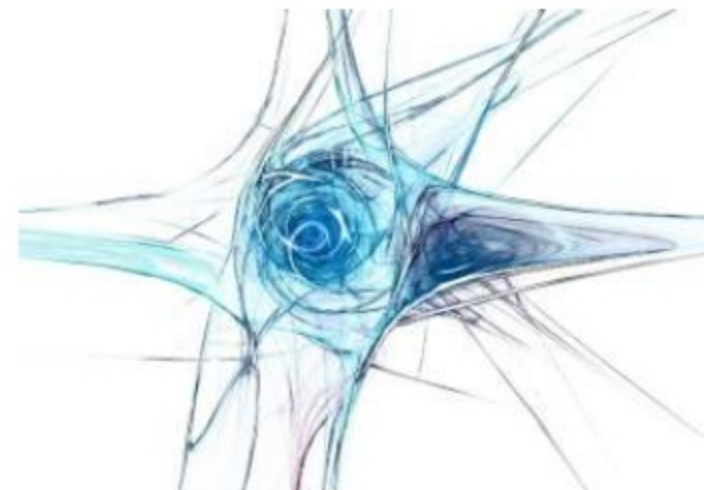
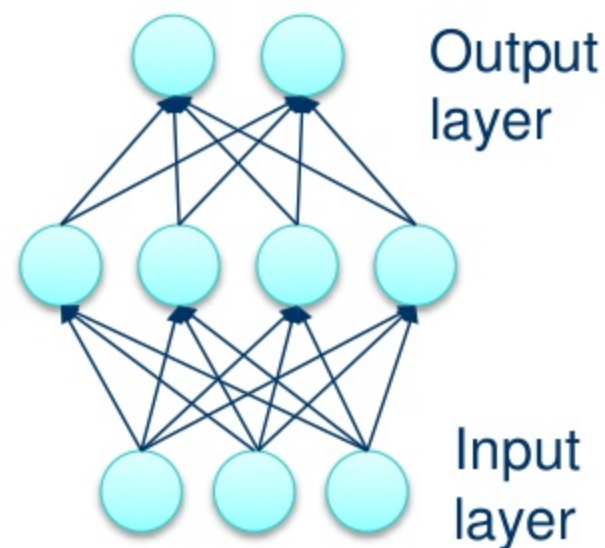


# Deep??

## Deep NN



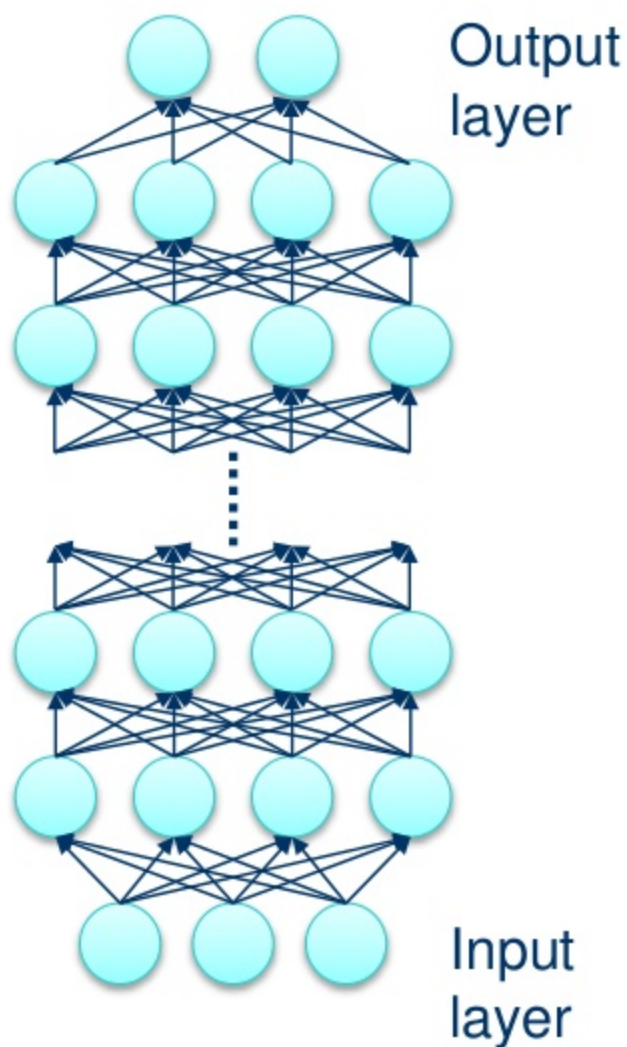
## (Shallow) NN





# Pros and Cons of Deep NN

## Deep NN



Until a few years ago...

1. Tend to be overfitting
2. Learning information does not reach to the lower layer

- Pre-training with RBM
- Big data

Image net

More than 1,5 M: Labeled images

<http://www.image-net.org/>

Labeled Faces in the Wild

More than 10,000: Face images

<http://vis-www.cs.umass.edu/lfw/>

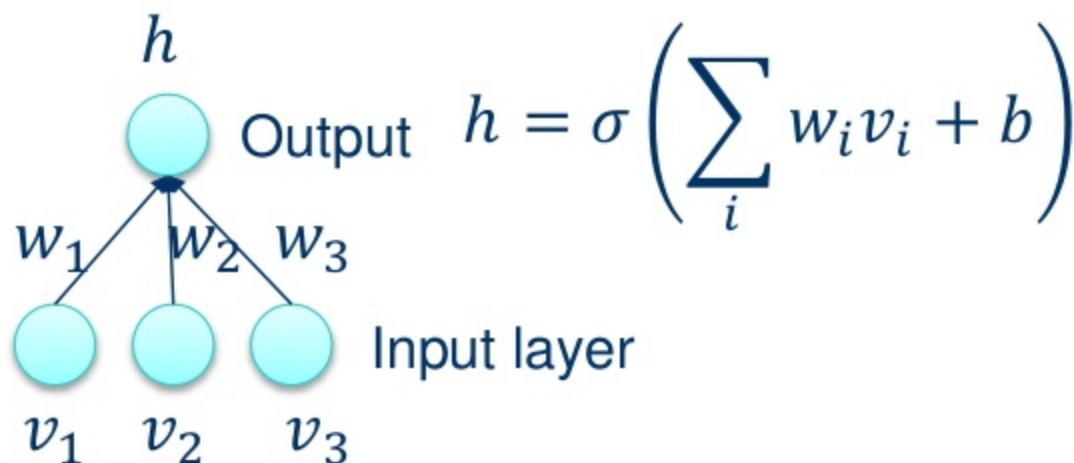
High-performance network



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# Single Layer Neural Network

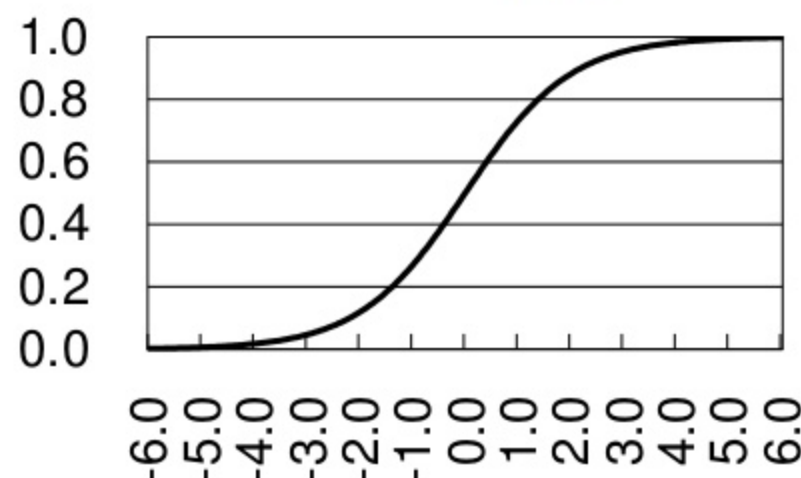
## ➤ Single node output



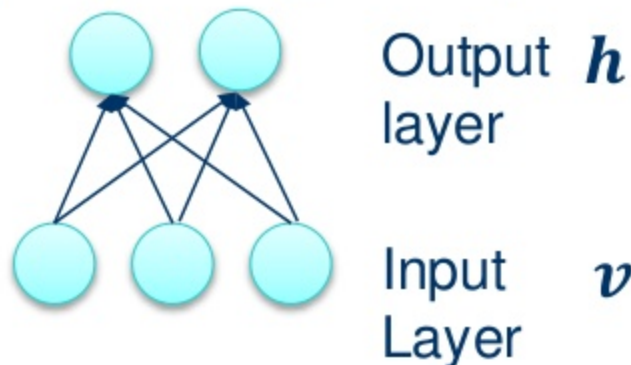
$$h = \sigma \left( \sum_i w_i v_i + b \right)$$

Sigmoid function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



## ➤ Multiple nodes output (Single Layer NN)



$$h_j = \sigma \left( \sum_i w_{ij} v_i + b_j \right)$$

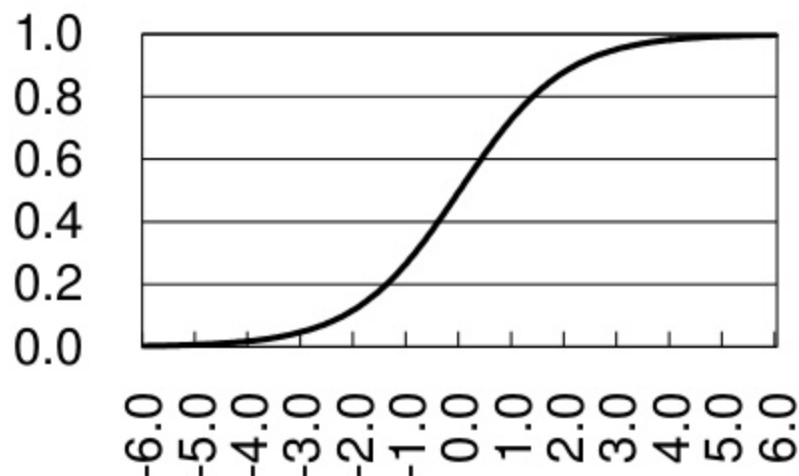
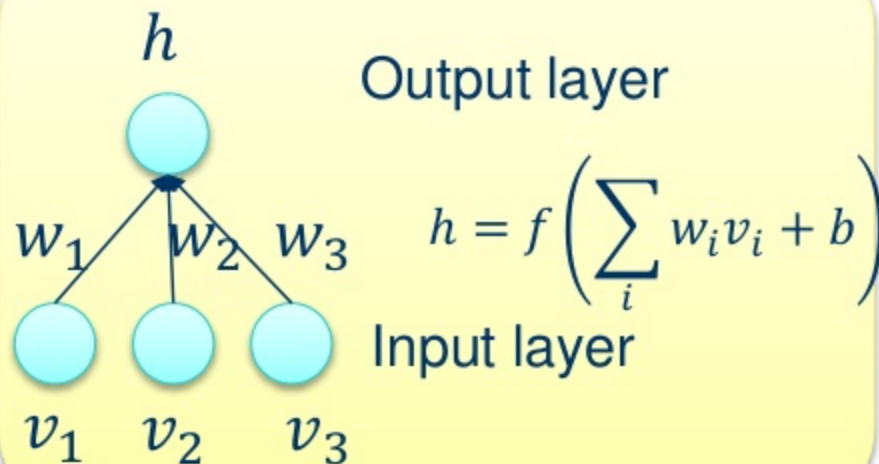
Vector representation of  
Single layer NN

$$\mathbf{h} = \sigma(\mathbf{W}^T \mathbf{v} + \mathbf{b})$$

It is equivalent to the  
inference model of the RBM

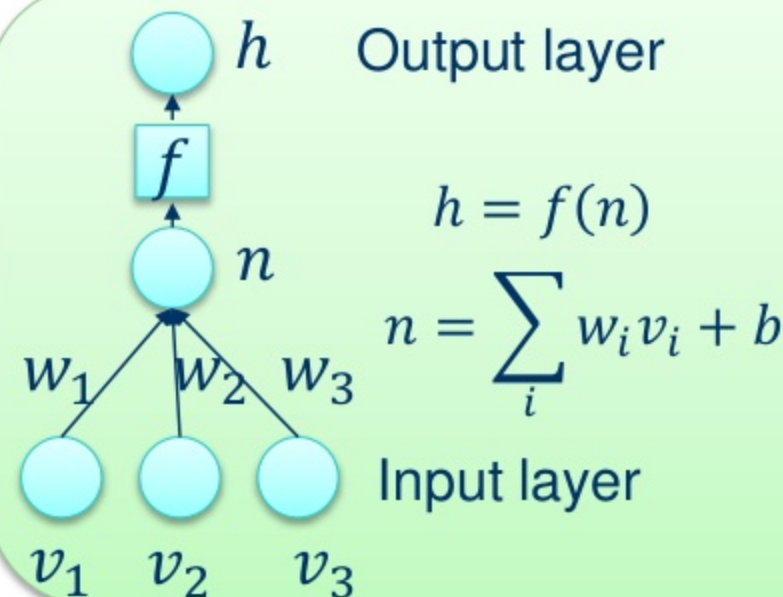
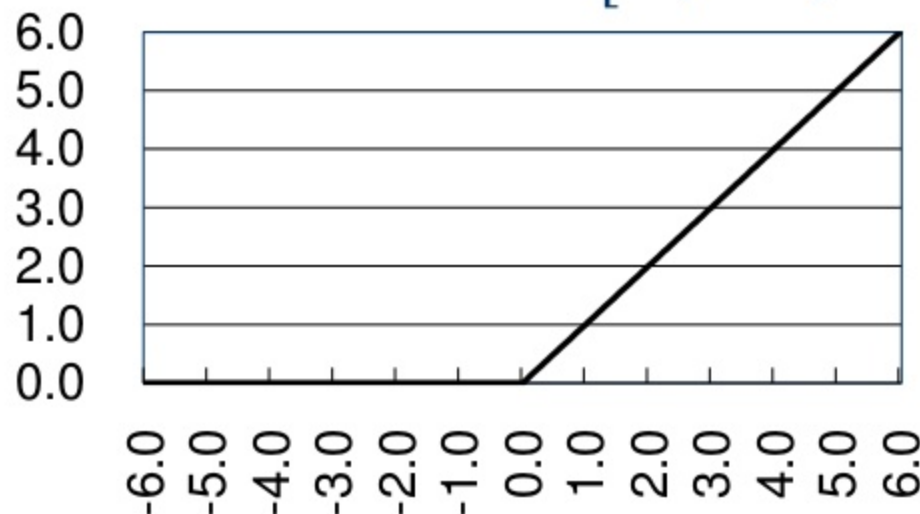
# Weighted sum and Activation functions

Sigmoid function  $f(x) = \sigma(x) = \frac{1}{1 + e^{-x}}$



Rectified linear unit

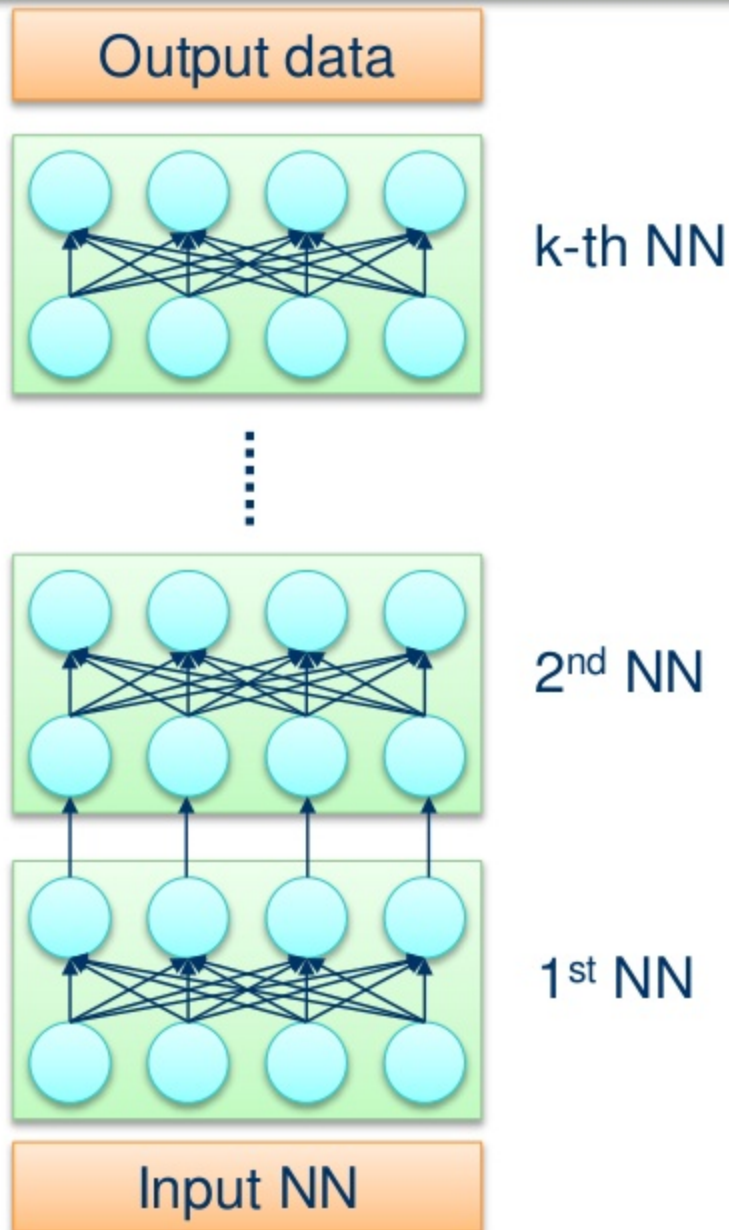
$$f(x) = \text{ReLU}(x) = \begin{cases} 0 & (x < 0) \\ x & (x \geq 0) \end{cases}$$





# Single layer NN to Deep NN

The deep NN is build up by stacking single layer NNs.



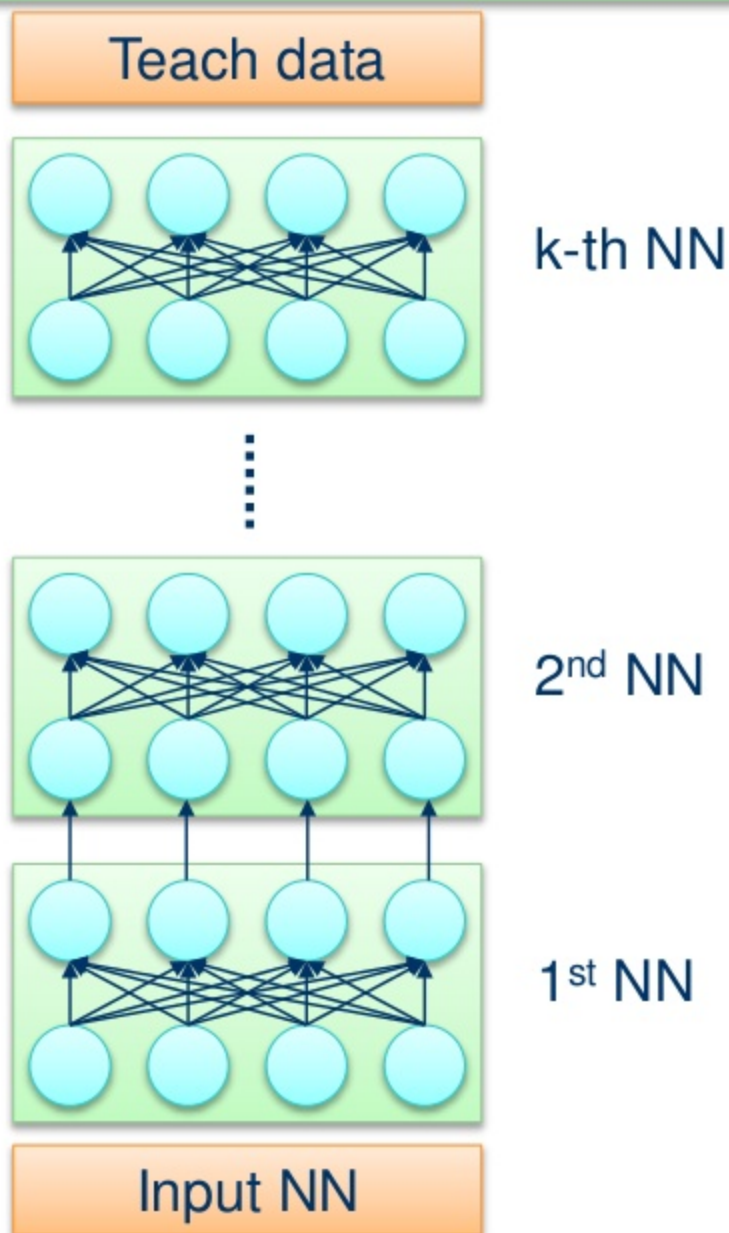
The output of the single layer NN will be the input of the next single layer NN.  
The output data of the deep NN is inferred by iterating the process.



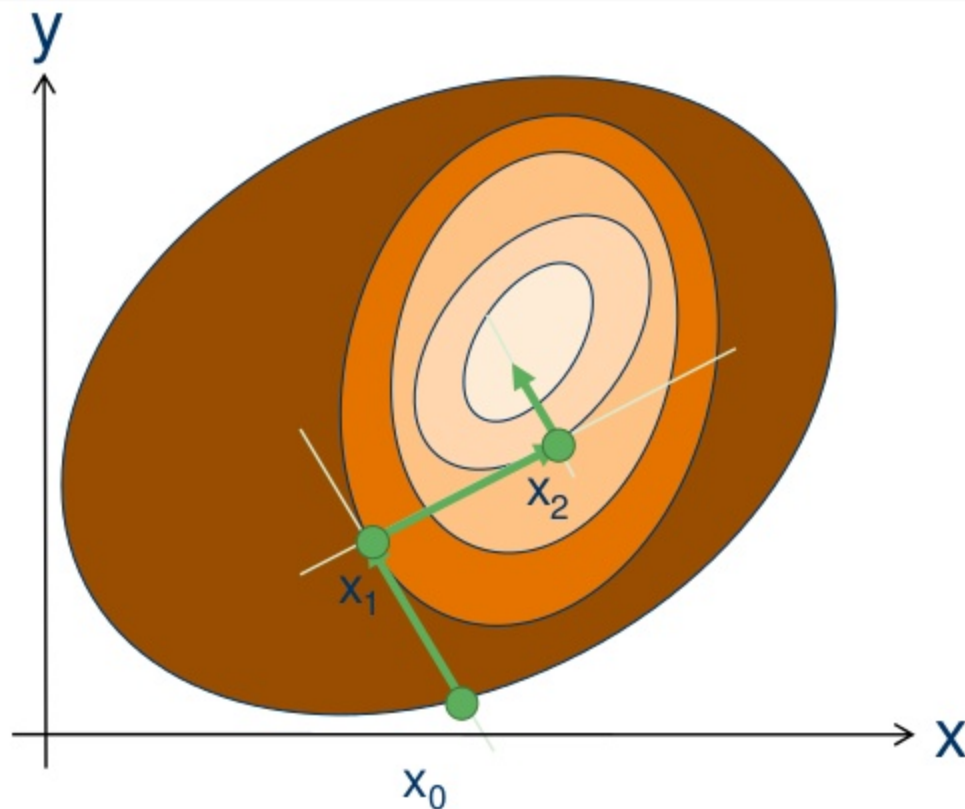
**TOKYO INSTITUTE OF TECHNOLOGY**

# Parameters estimation for deep NN

The deep NN is build up by stacking single layer NNs.



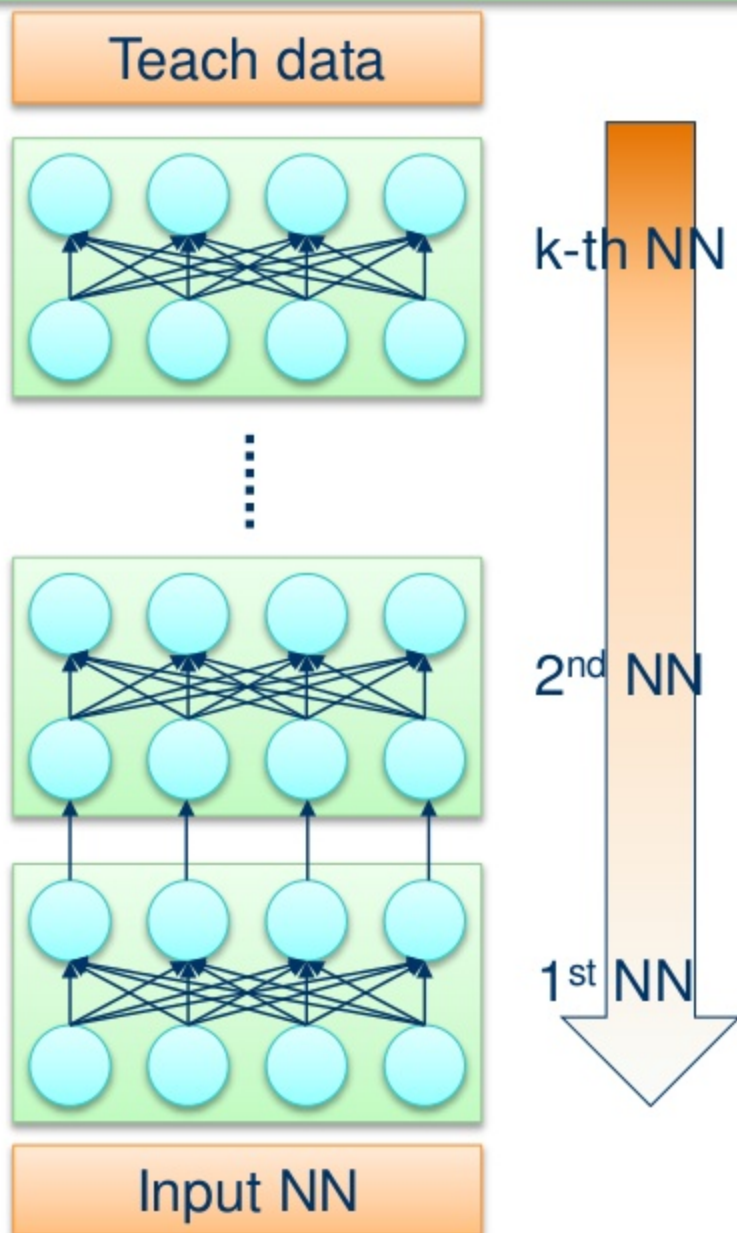
Parameters are estimated by gradient descent algorithm which minimizes the difference between the output data and teach data.





# Parameters estimation for deep NN

The deep NN is build up by stacking single layer NNs.



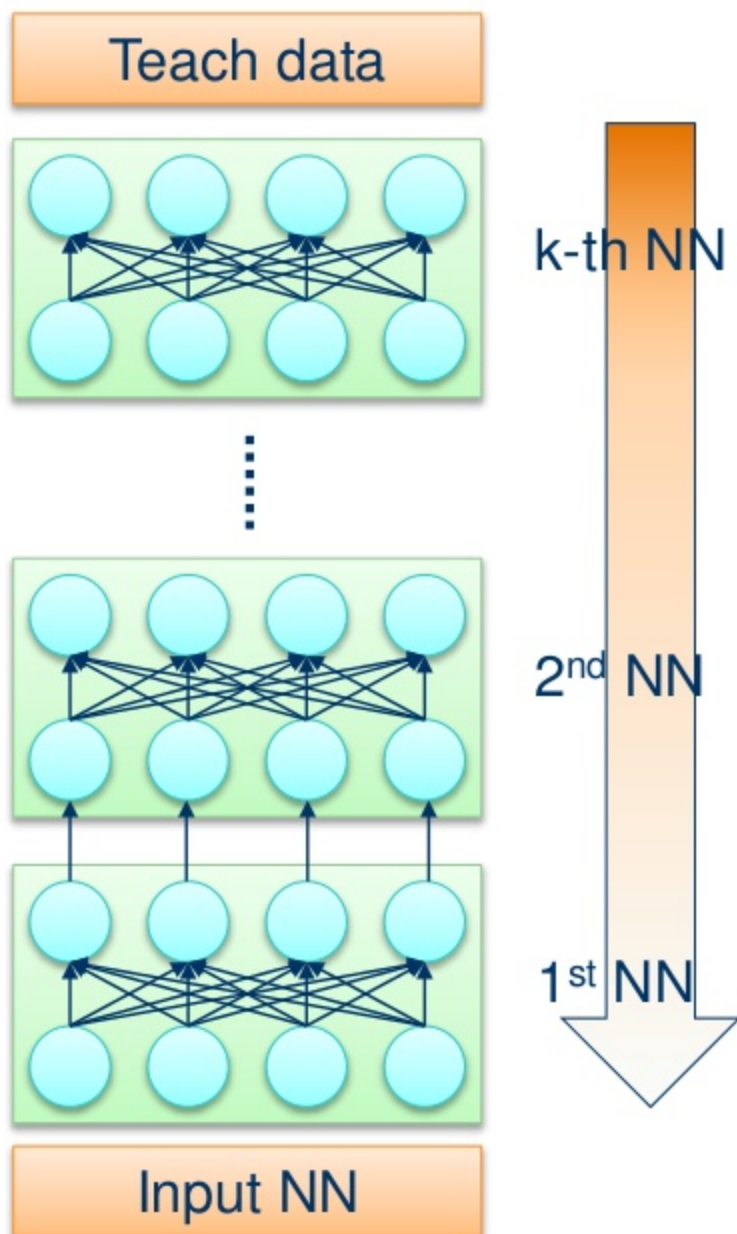
Parameters are estimated by gradient descent algorithm which minimizes the difference between the output data and teach data.

**Back-propagation:**  
The gradients can be calculated as propagating the information backward.





# Why the pre-training is necessary?



The back-propagation calculates the gradient from the output layer to the input layer.  
The information of the back-propagation can not reach the deep layers.

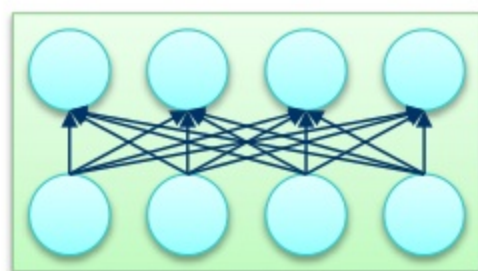
Deep layers (1<sup>st</sup> layer, 2<sup>nd</sup> layer, ...) are better to be learned by the unsupervised learning.



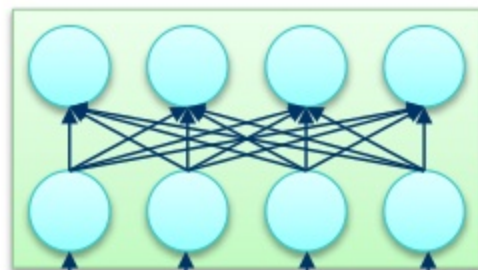
Pre-training with the RBMs.

# Pre-training with RBMs

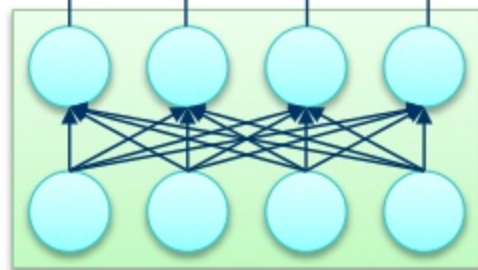
The inference of the single layer NN is mathematically equivalent to the inference of the RBM.



k-th NN

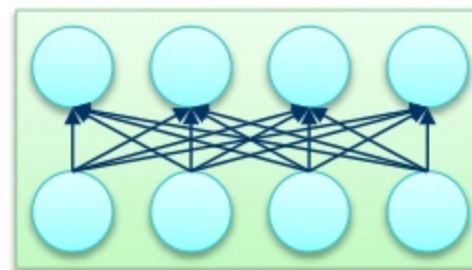


2<sup>nd</sup> NN

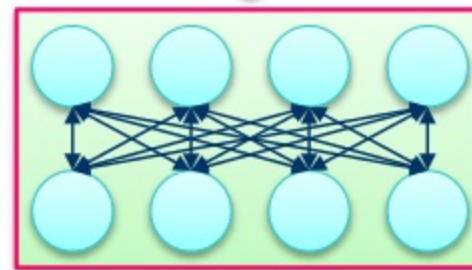


1<sup>st</sup> NN

Input data



Single layer NN



RBM

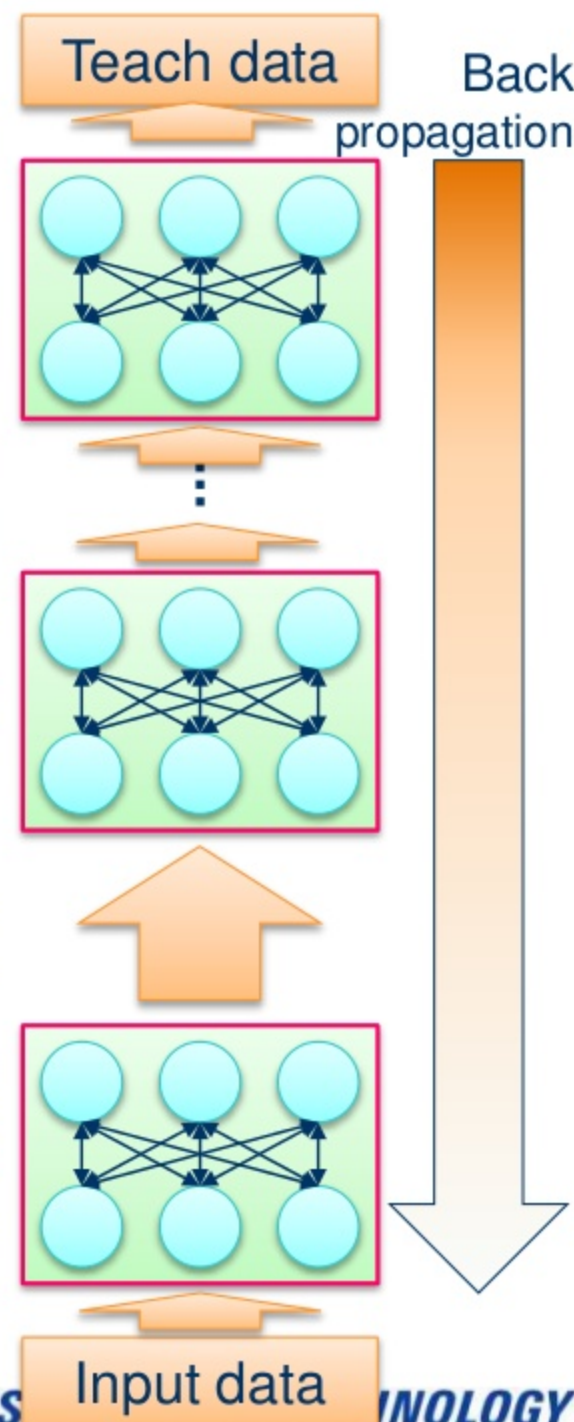
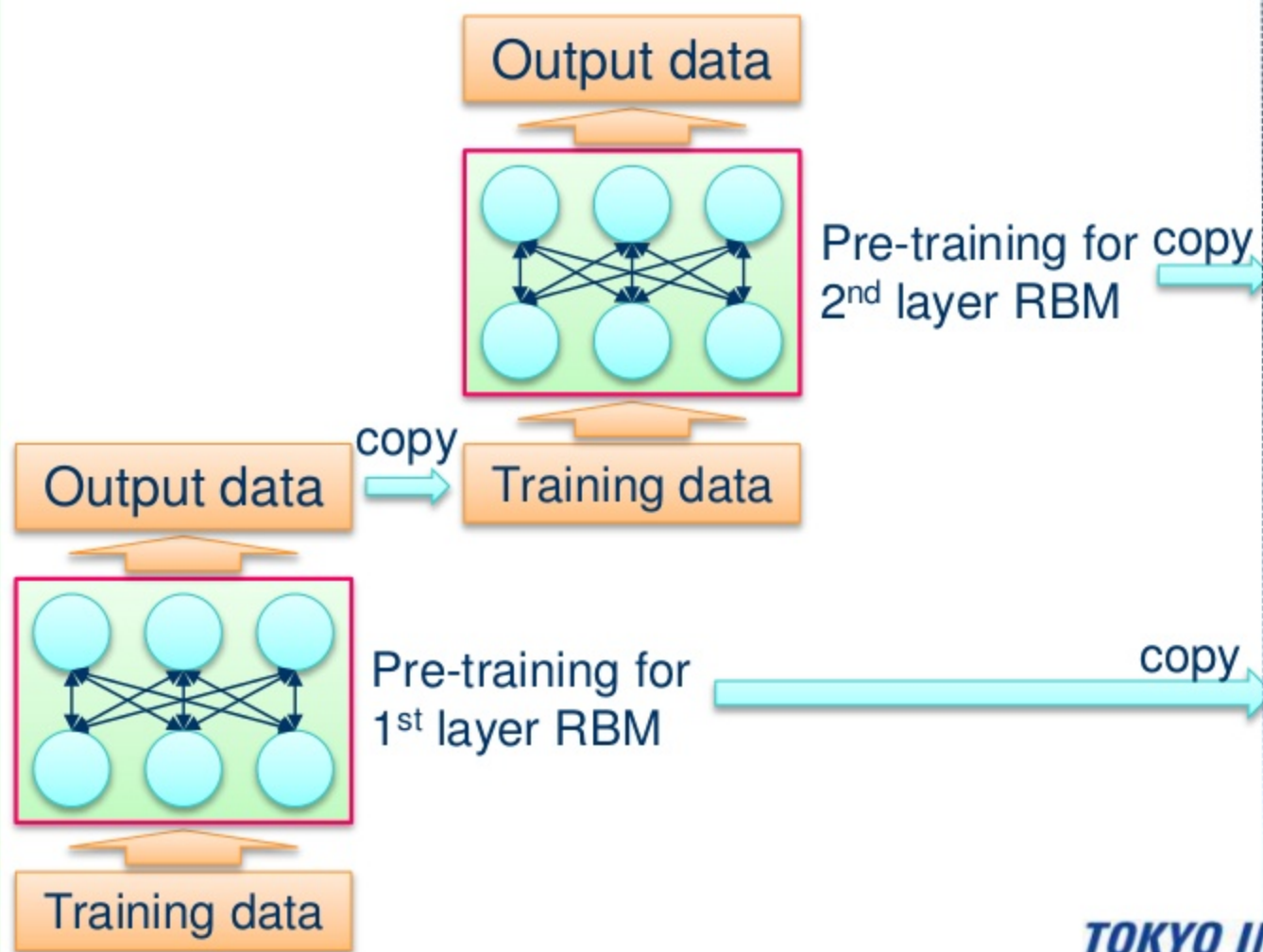
Data

The RBM parameters are estimated by maximum likelihood algorithm with given training data.

# Pre-training and fine-tuning

Fine-tuning of deep NN

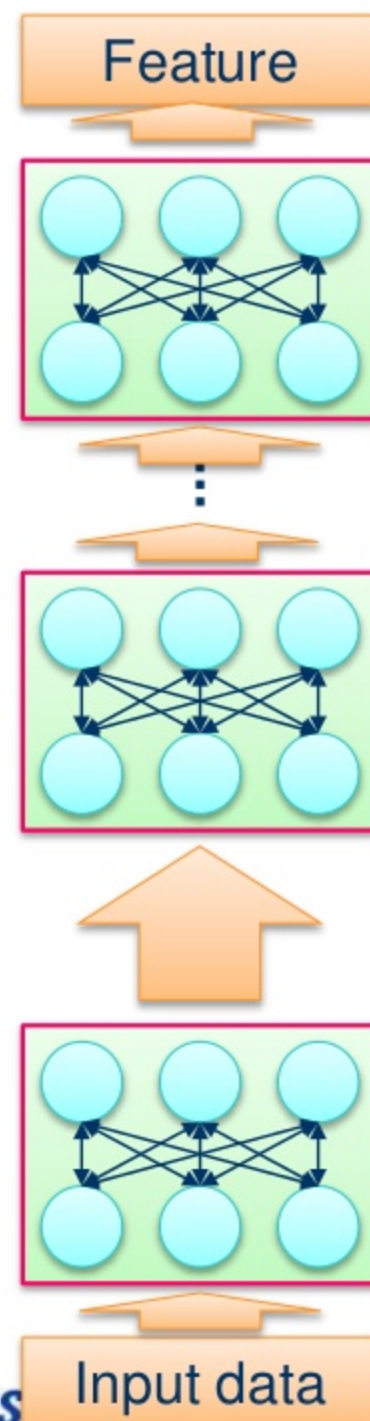
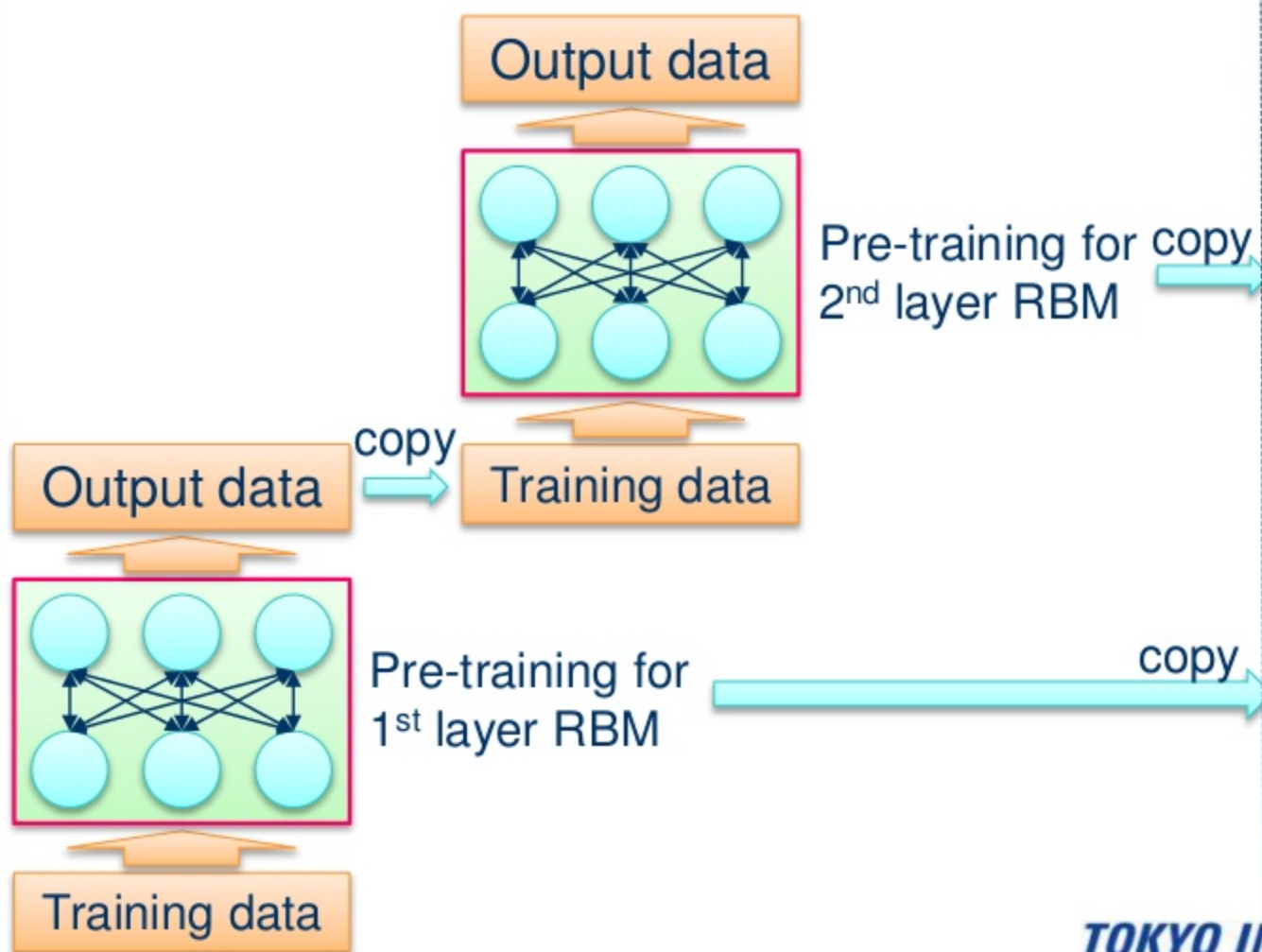
## Pre-training with RBMs





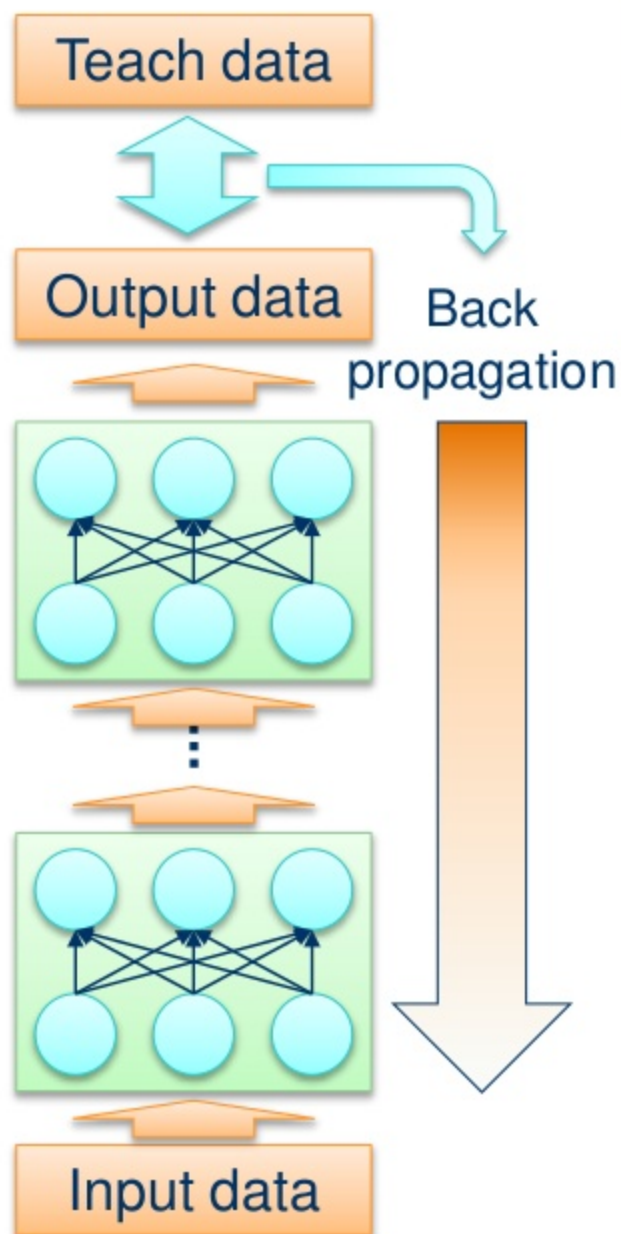
# Feature vector extraction

Pre-training with RBMs



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# Back-Propagation Algorithm



Vector representation of the single layer NN

$$h = \sigma(W^T v + b)$$

The goal of learning:

Weights  $W$  and bias  $b$  of the each layer are estimated, so that the differences between the output data and the teach data are minimized.

Objective function

$$I = \frac{1}{2} \sum_k \left( h_k^{(L)} - t_k \right)^2$$

Efficient calculation of the gradient  $\frac{\partial I}{\partial W^{(\ell)}}$  is important.

Back-propagation algorithm is an efficient algorithm to calculate the gradients.